# NEW YORK CITY COLLEGE OF TECHNOLOGY The City University of New York 

DEPARTMENT:
COURSE:

TITLE:

DESCRIPTION:

TEXT:

## CREDITS:

## PREREQUISITES:

Mathematics

MAT 2440
Discrete Structures and Algorithms I
This course introduces the foundations of discrete mathematics as they apply to computer science, focusing on providing a solid theoretical foundation for further work. Topics include functions, relations, sets, simple proof techniques, Boolean algebra, propositional logic, elementary number theory, writing, analyzing and testing algorithms.

Discrete Mathematics and its
Applications, $7^{\text {th }}$ edition
Kenneth H. Rosen
McGraw-Hill

3 (2 class hours, 2 lab hours)
CST 2403 and MAT 1375
Prepared by
Prof. A. P. Taraporevala
Fall 2011
A. Testing Guidelines:

The following exams should be scheduled:

1. A one-hour exam at the end of the First Quarter.
2. A one session exam at the end of the Second Quarter.
3. A one-hour exam at the end of the Third Quarter.
4. A one session Final Examination.
B. A Computer Algebra System (CAS) is used in class and for assignments (suggested problems are marked with an asterisk). This is a writing intensive course.

## Course Intended Learning Outcomes/Assessment Methods

| Learning Outcomes | Assessment Methods |
| :---: | :---: |
| 1. use the rules of logic to understand mathematical statements and prove propositions using <br> - A direct proof. <br> - An indirect proof. <br> - A proof by contradiction. <br> - Mathematical induction. | Classroom activities and discussion, homework, exams. |
| 2. Write simple algorithms using pseudocode. | Classroom activities and discussion, homework, exams. |
| 3. <br> - Traverse trees. <br> - Represent an expression using a binary tree and write it in prefix, postfix, and infix notation. <br> - Build spanning trees. | Classroom activities and discussion, homework, exams. |
| 4. Use computer technology to assist in the above. | Classroom activities and discussion, homework, exams. |

## General Education Learning Outcomes/Assessment Methods

| Learning Outcomes | Assessment Methods |
| :--- | :--- |
| 1. Gather, interpret, evaluate, and apply information <br> discerningly from a variety of sources. | Classroom activities and discussion, homework, <br> exams. |
| 2. Understand and employ both quantitative and <br> qualitative analysis to solve problems. | Classroom activities and discussion, homework, <br> exams. |
| 3. Employ scientific reasoning and logical thinking. | Classroom activities and discussion, homework, <br> exams. |
| 4. Communicate effectively using written and oral means. | Classroom activities and discussion, homework, <br> exams. |
| 5. Utilize computer based technology in accessing information, <br> solving problems and communicating. | Classroom activities and discussion, homework, <br> exams. |
| 6. Work with teams. Build consensus and use creativity. | Classroom activities and discussion, homework. |
| 7. Acquire tools for lifelong learning. | Classroom activities and discussion, homework, <br> exams. |

## Mathematics Department Policy on Lateness/ Absence

A student may be absent during the semester without penalty for $10 \%$ of the class instructional sessions. Therefore,

## If the class meets:

1 time per week
2 times per week

The allowable absence is:
2 absences per semester
3 absences per semester

Students who have been excessively absent and failed the course at the end of the semester will receive either

- the WU grade if they have attended the course at least once. This includes students who stop attending without officially withdrawing from the course.
- the WN grade if they have never attended the course.

In credit bearing courses, the WU and WN grades count as an F in the computation of the GPA. While WU and WN grades in non-credit developmental courses do not count in the GPA, the WU grade does count toward the limit of 2 attempts for a developmental course.

The official Mathematics Department policy is that two latenesses (this includes arriving late or leaving early) is equivalent to one absence.

Every withdrawal (official or unofficial) can affect a student's financial aid status, because withdrawal from a course will change the number of credits or equated credits that are counted toward financial aid.

## New York City College of Technology Policy on Academic Integrity

Students and all others who work with information, ideas, texts, images, music, inventions, and other intellectual property owe their audience and sources accuracy and honesty in using, crediting, and citing sources. As a community of intellectual and professional workers, the College recognizes its responsibility for providing instruction in information literacy and academic integrity, offering models of good practice, and responding vigilantly and appropriately to infractions of academic integrity. Accordingly, academic dishonesty is prohibited in The City University of New York and at New York City College of Technology and is punishable by penalties, including failing grades, suspension, and expulsion. The complete text of the College policy on Academic Integrity may be found in the catalog.

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| Week | Discrete Structures and Algorithms I | Homework |
| :---: | :---: | :---: |
| 1 | 1.1 Propositional Logic pages $1-12$ <br> 1.3 Propositional Equivalences pages $25-34$ Introduction to CAS | P. 12: 1, 2, 3, 6, 9, 11, 14, 23, 27 - 31, 37, 44 <br> P. 34: 3, 4, 6, 9 <br> Does MATLAB recognize irrational numbers? Why? Is the decimal representation a rational number? Is 1.55555... a rational number? Why? |
| 2 | 1.4 Predicates and Quantifiers pages $36-52$ <br> 1.5 Nested Quantifiers pages 57-64 <br> 1.6 Rules of Inference pages $69-78$ CAS Logic | P. 53: 1, 3, 4, 7 - 13 odd, 19, 30, 36 <br> P. 64: 10, 27, 31, 33 <br> P. 79: 19, 20, 35 (written assignment) |
| 3 | 1.7 Introduction to Proofs pages 80 - 90 <br> 2.1 Sets pages $115-125$ <br> 2.2 Set Operations pages $138-152$ CAS Sets | P. 91: $1-4,9-12,17,18,35$ <br> P. 125: 11, 19 (a) \& (b), 27, 29, 31, 35 <br> P. 136: 3, 15 (b), 17 (b), $21-23,26,46,47,49$ (written assignment), 52-55, 57 |
| 4 | First Examination <br> 2.3 Functions pages $133-146$ <br> CAS Floor and ceiling functions | P. 146: 3, 8, $10-12$ all, 15, 20 (written assignment), 23, 24, 30, 33, 39, 42 - 44, $58-61$ |
| 5 | 2.4 Sequences and Summations pages 156-167 <br> 2.5 Cardinality of Sets pages $170-176$ <br> 3.1 Algorithms pages 191-195 <br> CAS m-files (maximum, linear search) | P. 167: 3, 25, 29, 30, 31, 33, $35-39$ all, 43 <br> P. 176: $1,3,11$ <br> P. 177: 1, $3^{*}, 5^{*}, 7^{*}, 11^{*}, 13,14,16^{*}, 17^{*}, 18^{*}, 27^{*}$ |
| 6 | 3.1 Algorithms pages 196 - 198 MATLAB m-files (binary search) | P. 203: 34, 35, 36, 37*, $38-41$ all, 42*, 43* |
| 7 | 3.1 Algorithms pages $198-202$ <br> 4.1 Divisibility and Modular Arithmetic pages 237 - 244 <br> 4.2 Integer Representations and Algorithms pages 245-254 CAS m-files (bubble sort) | P. 208: 47, 48, 50, 52, 53, 57 (written assignment) <br> P. 244: 15, 21, 29, 26, 27, 28, 30*, 31, 32 <br> P. 255: 1 - 14 all, 25, 27, 32, 34, 47, 53*, 54, 55*, 56 |

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| Week | Discrete Structures and Algorithms I | Homework |
| :---: | :---: | :---: |
| 8 | Mid-semester Examination <br> 4.3 Primes and Greatest Common Divisor pages $257-272$ <br> 4.5 Applications of Congruences pages $287-292$ <br> 4.6 Cryptography pages $294-303$ <br> CAS m-files (insertion sort) | P. 272: 3, 16, 25, 28, 33, <br> P. 292: 2, 3, 6, $8^{*}$ <br> P. 304: 1 - 5 odd |
| 9 | 5.1 Mathematical Induction pages 311-329 5.2 Strong Induction and Well-Ordering pages 333 - 341 CAS m-files (Constructing Base b) | $\begin{aligned} & \text { P. 329: } 1,3-12,15,21,25 \\ & \text { P. 341: 7, 11, } 13 \end{aligned}$ |
| 10 | 5.3 Recursive Definitions and Structural Induction pages $344-357$ <br> 5.4 Recursive Algorithms pages $360-370$ <br> CAS m-files (Euclidean Algorithm) | P. 357: $1-7$ odd, 30, 33 - 35 all, 43, 44, MATLAB definition of Ackermann's function, 48*, 51*, 60, 61 <br> P. 370: 1 - 5 odd, $7^{*}, 8^{*}, 9^{*}, 10^{*}, 16,29,30,36^{*}, 46,50$, 51, 52* |
| 11 | 5.5 Program Correctness pages $372-376$ Third Examination | P. 377: 3, 7 |
| 12 | 10.1 Graphs and Graph Models pages 641-649 <br> 10.2 Graph Terminology and Special Types of Graphs pages 651-665 <br> 10.4 Connectivity pages 678 - 689 <br> CAS Recursive Algorithms | P. 649: 3-9 all, 33 <br> P. 665: 20, 59, 61, 67, 71, 72 <br> P. 689: $1-5$ all, 11 |
| 13 | 11.1 Introduction to Trees pages 745 - 755 <br> 11.2 Applications of Trees pages $757-769$ <br> 11.3 Tree Transversal pages $772-772$ <br> CAS Presentation | P. 755: $1-10$ all , $17-20$ all, 21 (written Assignment), 27, 28, 33, 34, $38-41$ all <br> P. 769: 1-7 odd, 11, 19, 21, 22, 37 <br> P. 783: 1, 3, 6, 7, 9, 10, 12, 13, 15, $22-24$ all |
| 14 | 11.4 Spanning Trees pages $785-795$ <br> 11.5 Minimum Spanning Trees pages $797-802$ (optional) CAS Presentation | $\begin{aligned} & \text { P. 795: } 2-6,13-15,16,27,28,30 \\ & \text { P. 802: } 1,2,3,6,7 \end{aligned}$ |
| 15 | Review/ CAS Presentation <br> Final Examination |  |

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| 3.1 Algorithms pages 196-198 CAS m-files (binary search) | P. 203: 34, 35, 36, 37*, $38-41$ all, 42*, 43* |
| 3.1 Algorithms pages 198 - 202 <br> 4.1 Divisibility and Modular Arithmetic pages 237-244 <br> 4.2 Integer Representations and Algorithms pages 245 - 254 CAS m-files (bubble sort) | P. 208: $47,48,50,52,53,57$ (written assignment) <br> P. 244: 15, 21, 29, 26, 27, 28, 30*, 31, 32 <br> P. 255: 1 - 14 all, 25, 27, 32, 34, 47, 53*, 54, 55*, 56 |

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| 5.1 Mathematical Induction pages 311 - 329 5.2 Strong Induction and Well-Ordering pages 333 - 341 CAS m-files (Constructing Base b) | $\begin{aligned} & \text { P. 329: } 1,3-12,15,21,25 \\ & \text { P. 341: } 7,11,13 \end{aligned}$ |
| 5.3 Recursive Definitions and Structural Induction pages 344 - 357 <br> 5.4 Recursive Algorithms pages 360 - 370 <br> CAS m-files (Euclidean Algorithm) | P. 357: $1-7$ odd, 30, $33-35$ all, 43, 44, MATLAB definition of Ackermann's function, 48*, 51*, 60, 61 <br> P. 370: 1 - 5 odd, $7^{*}, 8^{*}, ~ 9 *, ~ 10 *, ~ 16, ~ 29, ~ 30, ~ 36 *, ~ 46, ~ 50, ~$ 51, 52* |
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| Review/ CAS Presentation Final Examination |  |

